

```
> restart:with(linalg);
[BlockDiagonal, GramSchmidt, JordanBlock, LUdecomp, QRdecomp, Wronskian, addcol,
  addrow, adj, adjoint, angle, augment, backsub, band, basis, bezout, blockmatrix, charmat,
  charpoly, cholesky, col, coldim, colspace, colspan, companion, concat, cond, copyinto,
  crossprod, curl, definite, delcols, delrows, det, diag, diverge, dotprod, eigenvals,
  eigenvalues, eigenvectors, eigenvects, entermatrix, equal, exponential, extend, ffgausselim,
  fibonacci, forwardsub, frobenius, gausselim, gaussjord, geneqns, genmatrix, grad,
  hadamard, hermite, hessian, hilbert, htranspose, ihermite, indexfunc, innerprod, intbasis,
  inverse, ismith, issimilar, iszero, jacobian, jordan, kernel, laplacian, leastsqrs, linsolve,
  matadd, matrix, minor, minpoly, mulcol, mulrow, multiply, norm, normalize, nullspace,
  orthog, permanent, pivot, potential, randmatrix, randvector, rank, ratform, row, rowdim,
  rowspace, rowspan, rref, scalarmul, singularvals, smith, stackmatrix, submatrix, subvector,
  sumbasis, swapcol, swaprow, sylvester, toeplitz, trace, transpose, vandermonde, vecpotent,
  vectdim, vector, wronskian]
```

```
> R:=-x*y+2*y^2;S:=-x^2*y;
      R := -x y + 2 y^2
      S := -x^2 y
```

```
> x:=(U+V)/2;y:=(U-V)/(2*I);
      x := 1/2 U + 1/2 V
      y := -1/2 I (U - V)
```

```
> G:=simplify(R+I*S);
      G := 1/4 I U^2 - 1/4 I V^2 - 1/2 U^2 + U V - 1/2 V^2 - 1/8 U^3 - 1/8 U^2 V + 1/8 U V^2 + 1/8 V^3
```

```
> g[20]:=diff(G,U,U);
      g20 := -1 + 1/2 I - 3/4 U - 1/4 V
```

```
> g[11]:=diff(G,U,V);
      g11 := 1 - 1/4 U + 1/4 V
```

```
> g[21]:=diff(G,U,U,V);
      g21 := -1/4
```

```
> U:=0;V:=0;
      U := 0
      V := 0
```

```
> g[20]:=eval(g[20]);g[11]:=eval(g[11]);g[21]:=eval(g[21]);
      g20 := -1 + 1/2 I
```

$$g_{11} := 1$$

$$g_{21} := -\frac{1}{4}$$

(9)

> l[1] := (1/2) * Re (I * g[20] * g[11] + g[21]) ;

$$l_1 := -\frac{3}{8}$$

(10)