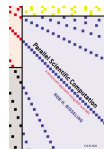
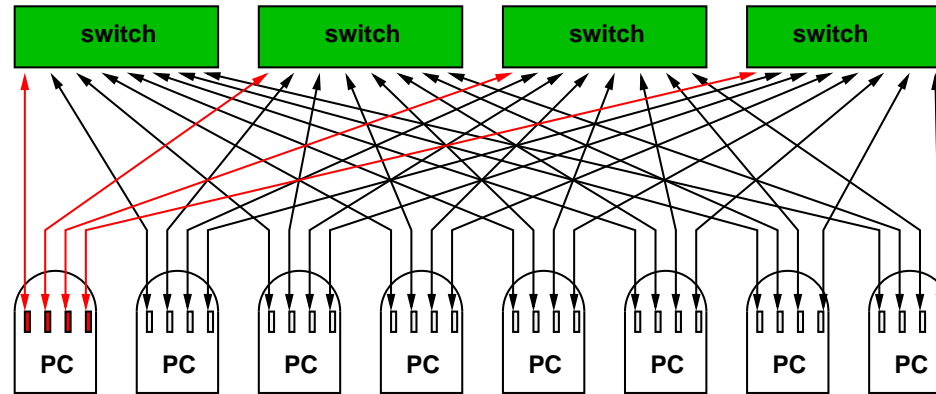


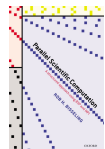
Experimental results on a Beowulf cluster **(PSC §4.10)**



Beowulf cluster



- A **Beowulf cluster** consists of several PCs connected by communication switches.
- We use a cluster of 32 IBM x330 nodes, located at the Physics Department of Utrecht University, part of DAS-2, the 200-node Distributed ASCI Supercomputer built by 5 collaborating Dutch universities.
- Each node contains 2 Pentium-III processors with 1 GHz clock speed, 1 Gbyte of memory, and a local disk.
- Nodes are connected by a Myrinet-2000 network.

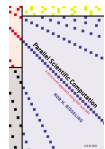


Panda BSP library

p	g	l	$T_{\text{comm}}(0)$
1	1337	7 188	6 767
2	1400	100 743	102 932
4	1401	226 131	255 307
8	1190	440 742	462 828
16	1106	835 196	833 095
32	1711	1 350 775	1 463 009
64	2485	2 410 096	2 730 173

Benchmarked BSP parameters p, g, l and time of a 0-relation ($r = 323$ Mflop/s)

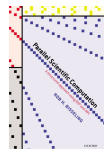
- Experimental BSP library **on top of** Panda portability layer **on top of** Myrinet.
- 2 processors per node; for $p \leq 32$, only 1 is used.



Test set of sparse matrices

Matrix	n	nz	Origin
random20k	20 000	99 601	random sparse matrix
amorph20k	20 000	100 000	amorphous silicon
prime20k	20 000	382 354	prime number matrix
bcsstk32	44 609	2 014 701	automobile chassis
cage12	130 228	2 032 536	DNA electrophoresis

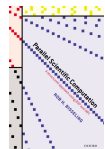
(Subset of the original test set from Section 4.10)



BSP cost for smaller matrices

p	random20k	amorph20k	prime20k
1	199 202	200 000	764 708
2	102 586 + 5073 $_g$	100 940 + 847 $_g$	393 520 + 4275 $_g$
4	51 292 + 4663 $_g$	51 490 + 862 $_g$	196 908 + 5534 $_g$
8	25 642 + 3452 $_g$	25 742 + 1059 $_g$	98 454 + 4030 $_g$
16	12 820 + 2152 $_g$	12 872 + 530 $_g$	49 226 + 3148 $_g$
32	6 408 + 1478 $_g$	6 434 + 371 $_g$	24 612 + 2620 $_g$
64	3 202 + 1007 $_g$	3 216 + 267 $_g$	12 304 + 2235 $_g$

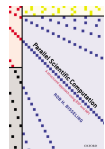
- Matrix and vectors partitioned by **Mondriaan**.
- Fixed synchronisation cost $4l$ not shown. Since $l \approx 100\,000$ for $p = 2$, matrices must have **at least 100 000 nonzeros** to make parallelism worthwhile.



BSP cost for larger matrices

p	bcsstk32	cage12
1	4 029 402	4 065 072
2	2 070 816 + 630 $_g$	2 093 480 + 10 389 $_g$
4	1 036 678 + 786 $_g$	1 046 748 + 15 923 $_g$
8	518 676 + 842 $_g$	523 376 + 16 543 $_g$
16	259 390 + 1163 $_g$	261 684 + 9 984 $_g$
32	129 692 + 917 $_g$	130 842 + 6 658 $_g$
64	64 836 + 724 $_g$	65 420 + 5 385 $_g$

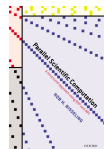
- Same number of nonzeros, but much more communication for cage12.
- This may be due to the high-dimensional underlying structure of cage12, in contrast to bcsstk32, which is only 3D.



Measured execution time (in ms)

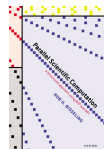
p		random 20k	amorph 20k	prime 20k	bcsstk32	cage12
1	(seq)	9	7	18	71	92
1	(par)	10	8	19	72	96
2		73	13	56	59	205
4		57	16	77	39	228
8		48	15	50	25	226
16		32	11	46	24	128
32		28	17	37	23	87
64		36	29	45	34	73

- Compare random20k and amorph20k: same size and number of nonzeros, but amorph20k much faster.
- Only modest speedups obtained for larger problems.



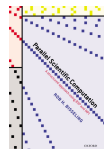
Did we gain something?

- We have shown that for large problem sizes the algorithm scales well.



Did we gain something?

- We have shown that for large problem sizes the algorithm scales well.
- Many research papers on parallel computing end like this, even if the statement is not true.
- The sad truth: we haven't reached the problem size yet where parallel computing becomes worthwhile. The high value $g \approx 1000$ hinders obtaining decent speedups.
- Our main goal should be to understand the results, whatever they may be.



Summary

- Clusters of PCs are cheap supercomputers with **tremendous potential**.
- BSPlib implementations for such clusters can have great impact. The Panda BSP library is one such library. But networks evolve fast and form a moving target.
- Top of my wish list: **new implementations** for clusters based on Infiniband, Fast Ethernet, etc., and for dual-core and multi-core PCs. Preferably open-source.
- 20 years from now:
 - Blue Gene, Earth Simulator, DAS-2, and their friends will all be dead
 - I shall be older and perhaps wiser
 - BSP costs like $65\,420 + 5\,385g + 4l$ for matrix `cage12` will still be meaningful, as predictors for **Exaflop/s** (10^{18} flop/s) machines.

