

15a. Shift operators

Check of (3.78)

```
In[ = ]:= Clear[h, p, r]
sh[3, 1, phi[h, p, r, p, nu], subtriv]/phi[h+3, p+1, r+1, p+1, nu] // Simplify
sh[-3, 1, phi[h, p, r, p, nu], subtriv]/phi[h-3, p+1, r-1, p+1, nu] // Simplify
Out[ = ]= 
$$\frac{(4 + h + 2 \nu + 2 p - r) \times (2 + p + r)}{8 \times (1 + p)}$$

In[ = ]:=
sh[3, -1, phi[h, p, r, p, nu], subtriv]/phi[h+3, p-1, r+1, p-1, nu] // Simplify
sh[-3, -1, phi[h, p, r, p, nu], subtriv]/phi[h-3, p-1, r-1, p-1, nu] // Simplify
Out[ = ]= 
$$-\frac{p (-h - 2 \nu + 2 p + r)}{4 \times (1 + p)}$$

Out[ = ]= 
$$-\frac{p (h - 2 \nu + 2 p - r)}{4 \times (1 + p)}$$

```