

## 23c) Part ii)

Take  $\varepsilon = 1$ .

```
In[ ]:= j1 + nu1 ≤ -2 - 2 m0[j1] /. m0sub[jp] /. eps → 1 // . sub2p // Simplify
```

```
Out[ ]:= 1 + m0[jp] ≤ 0
```

So  $m_0(j_l)$  is the sole non-negative  $m_0(j)$ .

The basis point of  $\text{Sect}(j_l)$  satisfies the condition in Lemma 4.15.

The highest point satisfying the condition :

```
In[ ]:= Clear[b1]
```

```
j1 + nu1 == -2 - 2 b1 // . sub2p // Simplify
```

```
Solve[%, {b1}][[1]]
```

```
2 j1 + 3 (b1 + 1) == 2 jp - 3 (b1 + 1) /. % // . sub2p // Simplify
```

```
Out[ ]:= 2 + 2 b1 == jp + nup
```

```
Out[ ]:= {b1 →  $\frac{1}{2} \times (-2 + jp + nup)$ }
```

```
Out[ ]:= True
```

So the highest point is one step lower than the left boundary of the sector  $\text{Sector}(j_+)$ .

```
Out[ ]:= Take  $\varepsilon = -1$ .
```

```
In[ ]:= -jr + nur ≤ -2 - 2 m0[jr] /. m0sub[jp] /. eps → -1 // . sub2p // Simplify
```

```
Out[ ]:= 1 + m0[jp] ≤ 0
```

Only the sector  $\text{Sect}(j_r)$  to be considered ,

Highest point on the left boundary of  $\text{Sect}(j_r)$  that satisfies the condition in iv) in Lemma 4.15.

```
In[ ]:= Clear[b1]
```

```
nur - jr == -2 - 2 b1 // . sub2p // Simplify
```

```
Solve[%, {b1}][[1]]
```

```
b = b1 + 1 /. %
```

```
Out[ ]:= 2 + 2 b1 + jp == nup
```

```
Out[ ]:= {b1 →  $\frac{1}{2} \times (-2 - jp + nup)$ }
```

```
Out[ ]:=  $1 + \frac{1}{2} \times (-2 - jp + nup)$ 
```

```
In[ ]:= 2 jr - 3 b == 2 jp + 3 b // . sub2p // Simplify
```

```
Out[ ]:= True
```

So we can go up to one step below  $\text{Sect}(j_+)$ .