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## 25 Sesquilinear forms and unitarity

Computations for section 4.5

### Preparation

Definition of  $c$  in (4.91).

```
In[ ]:= Clear[c, j, nu]
c[p_, r_, nu_] = Gamma[1 + (j - nu + p + r) / 2] Gamma[1 + (-j - nu + p - r) / 2]
Gamma[1 + (j + nu + p + r) / 2]^(-1) Gamma[1 + (-j + nu + p - r) / 2]^(-1);
```

The function  $c$  determines an invariant form. The question is whether it, or a holomorphic multiple of it, is positive definite on submodules, in which the  $K$ -types are  $(\tau^h)_p$  with  $h = h_0 + 3(a - b)$  and  $p = p_0 + a + b$ .

```
In[ ]:= Clear[a, b, h, p, r, h0, r0, p0, lsub0, lsub]
lsub0[h0_, p0_] = {h → h0 + 3(a - b), p → p0 + a + b, r → (h - 2j) / 3};
lsub[h0_, p0_] := Union[lsub0[h0, p0], {Gamma[aa_] → Factorial[aa - 1]}];
```

```
In[ ]:=
Clear[gamsub]
gamsub[xx_] := Gamma[xx] → Pi Gamma[1 - xx]^(-1) Sin[Pi xx]^(-1)
```

25a. Type  $II_+$

25b. Comparison of Tables 4.3 and 4.14

25c. Types IF and FI

25d. Type FF